

# Identità goniometriche

risolubili mediante le relazioni fondamentali

1	$\frac{1 + \sin \alpha \cos \alpha}{\sin \alpha} = \cosec \alpha + \frac{1}{\sec \alpha}$
2	$\frac{\sin \alpha \cos \alpha - 1}{\cos \alpha} = \frac{1}{\cosec \alpha} - \sec \alpha$
3	$\frac{(1 - \cos \alpha)(\cos^2 \alpha + \cos \alpha + 1)}{\cos \alpha} = \frac{2 \sin^2 \alpha - \sin^4 \alpha - 1}{\cos^2 \alpha} + \frac{1}{\cos \alpha}$
4	$\frac{\cos \alpha}{1 - \sin^2 \alpha} + \cosec \alpha = \sin \alpha + \sec \alpha + \frac{1 - \sin^2 \alpha}{\sin \alpha}$
5	$\frac{1}{\cot \alpha} + \frac{\sin^2 \alpha - 1}{\cos^3 \alpha} = \frac{1 - \sin \alpha - \cos^2 \alpha}{\sin \alpha \cos \alpha}$
6	$\frac{1}{\tan \alpha} - \frac{1}{\sec \alpha} = \frac{\cos \alpha(1 - \sin \alpha)}{\sin \alpha}$
7	$\frac{1}{\cos \alpha(1 + \tan^2 \alpha)} + \frac{1}{\cosec \alpha} = \cos \alpha(\tan \alpha + 1)$
8	$\sin^2 \alpha + \tan \alpha = \frac{\sec \alpha(1 - \cos^2 \alpha)}{\sin \alpha} + \frac{\cos^2 \alpha - \cos^4 \alpha}{1 - \sin^2 \alpha}$
9	$\frac{1}{1 + \tan^2 \alpha} + \frac{1}{\cosec \alpha} = \sin \alpha + \frac{1}{\sec^2 \alpha}$
10	$\cot \alpha + \frac{\sin^2 \alpha + \sin \alpha - 1}{\sin \alpha \cos \alpha} = \frac{\cos \alpha}{1 - \sin^2 \alpha}$
11	$\sec \alpha - \cos \alpha = \frac{\sin^2 \alpha}{\cos \alpha}$
12	$\frac{2 \cos^2 \alpha - 1}{1 - \sin^2 \alpha} = 1 - \tan^2 \alpha$
13	$\frac{\sin^2 \alpha + \tan^2 \alpha}{1 - \cos^4 \alpha} = \sec^2 \alpha$
14	$\frac{\tan^2 \alpha + 1}{\tan^2 \alpha - 1} = \frac{\tan \alpha + \cot \alpha}{\tan \alpha - \cot \alpha}$
15	$\sin^3 \alpha = (\cos \alpha - \cos^3 \alpha) \tan \alpha$
16	$\frac{\sin^2 \alpha + \tan^2 \alpha}{1 - \cos^4 \alpha} = \sec^2 \alpha$
17	$\frac{\cos^2 \alpha - \cos \alpha - 1}{\sin \alpha} + \cot \alpha = \frac{\sin^3 \alpha - \sin \alpha}{\cos^2 \alpha}$
18	$\frac{1}{2 \cos^2 \alpha - 1} = \frac{1 + \tan^2 \alpha}{1 - \tan^2 \alpha}$
19	$\frac{1 + \sin \alpha}{\cot \alpha + \cos \alpha} = \frac{\tan \alpha + \sin \alpha}{1 + \cos \alpha}$
20	$(\sec \alpha + \tan \alpha)^2 = \frac{1 + \sin \alpha}{1 - \sin \alpha}$

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risolubili mediante angoli associati

21	$\sin^2(\pi - \alpha) + \cos(\pi - \alpha) = 1 - \cos \alpha - \cos^2 \alpha$
22	$\sin^4(\pi - \alpha) = \cos^4 \alpha - 1 + 2 \sin^2(\pi - \alpha)$
23	$1 + \sin \alpha - \sec(\pi - \alpha) \cos(\pi - \alpha) = \sin(\pi - \alpha) \sec \alpha \cos \alpha$
24	$\frac{\operatorname{ctg} \alpha}{\cos^2(\pi - \alpha)} = \operatorname{tg} \alpha - \operatorname{ctg}(\pi - \alpha)$
25	$\cos \alpha - \sin \alpha = \frac{\cos^2(\pi - \alpha) - \sin^2(\pi - \alpha)}{\sin(\pi - \alpha) - \cos(\pi - \alpha)}$
26	$\sin^2(\pi - \alpha) - \cos(\pi - \alpha) - \sin \alpha \operatorname{tg}(\pi - \alpha) = \sec \alpha + 1 - \cos^2(\pi - \alpha)$
27	$\operatorname{ctg}^2 \alpha + \frac{1 + 2 \cos(\pi + \alpha)}{\sin^2(\pi + \alpha)} = \frac{1 + \cos(\pi + \alpha)}{1 - \cos(\pi + \alpha)}$
28	$-\cos(\pi + \alpha) - \sec \alpha = \sin(\pi + \alpha) \operatorname{tg}(\pi + \alpha)$
29	$1 + \operatorname{tg} \alpha = \operatorname{tg} \alpha [1 + \operatorname{ctg}(\pi + \alpha)]$
30	$\operatorname{ctg}(\pi + \alpha) + \operatorname{tg} \alpha = \frac{1}{\sin(\pi + \alpha) \cos(\pi + \alpha)}$
31	$\operatorname{ctg}^2(\pi + \alpha) = \frac{1 + \operatorname{ctg}^2(\pi + \alpha)}{1 + \operatorname{tg}^2(\pi + \alpha)}$
32	$\frac{\sec^2(\pi + \alpha)}{\operatorname{cosec}(\pi + \alpha)} = [\operatorname{tg}(\pi + \alpha) + \operatorname{ctg} \alpha] \frac{\sec(\pi + \alpha)}{\operatorname{cosec}^2 \alpha}$
33	$\operatorname{cosec}(2\pi - \alpha) = -\cos(2\pi - \alpha) \operatorname{ctg} \alpha - \sin \alpha$
34	$\sin(2\pi - \alpha) \operatorname{ctg}(2\pi - \alpha) + 1 = -\frac{\sin \alpha + \operatorname{tg} \alpha}{\operatorname{tg}(2\pi - \alpha)}$
35	$\frac{\cos(2\pi - \alpha)}{1 + \sin(2\pi - \alpha)} = \frac{1 - \sin(2\pi - \alpha)}{\cos(2\pi - \alpha)}$
36	$\sin(2\pi - \alpha) \operatorname{tg}(2\pi - \alpha) = \sec(2\pi - \alpha) - \cos(2\pi - \alpha)$
37	$\frac{\sin(2\pi - \alpha)}{\sec^2(2\pi - \alpha)} = \frac{\cos(2\pi - \alpha)}{\operatorname{ctg}(2\pi - \alpha) + \operatorname{tg}(2\pi - \alpha)}$
38	$\operatorname{ctg} \alpha = \frac{\sin(2\pi - \alpha)}{1 - \cos(-\alpha)} - \operatorname{cosec}(2\pi - \alpha)$
39	$\frac{1 + \operatorname{tg}^2(-\alpha)}{1 - \operatorname{tg}^2(2\pi - \alpha)} = \frac{1}{2 \cos^2(-\alpha) - 1}$
40	$\frac{\cos(2\pi - \alpha)}{1 - \sin(-\alpha)} = \operatorname{tg}(-\alpha) + \sec(2\pi - \alpha)$

# Identità goniometriche

risolubili mediante formule goniometriche

41	$\sin(\alpha + \beta) \sin(\alpha - \beta) = \sin^2 \alpha - \sin^2 \beta$
42	$\sin \alpha \cos(\alpha + \beta) = \cos \alpha \sin(\alpha + \beta) - \cos \beta$
43	$\sin \alpha \sin(\alpha - \beta) + \cos \alpha \cos(\alpha - \beta) = \cos \beta$
44	$\frac{\cos(\alpha + \beta) + \cos(\alpha - \beta)}{\sin(\alpha + \beta) + \sin(\alpha - \beta)} = \operatorname{ctg} \alpha$
45	$\frac{\cos(\alpha - \beta)}{\cos(\alpha + \beta)} = \frac{1 + \operatorname{tg} \alpha \operatorname{tg} \beta}{1 - \operatorname{tg} \alpha \operatorname{tg} \beta}$
46	$\cos(\alpha - \beta) = (\operatorname{tg} \alpha + \operatorname{ctg} \beta) \sin \beta \cos \alpha$
47	$(\operatorname{tg} \alpha + \operatorname{tg} \beta)[\cos(\alpha + \beta) + \cos(\alpha - \beta)] = 2 \sin(\alpha + \beta)$
48	$\sin 11\alpha - \sin \alpha = 2 \cos 6\alpha \sin 5\alpha$
49	$\frac{\cos 4\alpha - \cos 8\alpha}{\cos 4\alpha + \cos 8\alpha} = \operatorname{tg} 6\alpha \operatorname{tg} 2\alpha$
50	$2 \cos 2\alpha \cos 3\alpha = \cos 5\alpha + \cos \alpha$
51	$\frac{\sin 3\alpha + \sin \alpha}{\sin 5\alpha - \sin \alpha} = \cos \alpha \sec 3\alpha$
52	$\cos^2 4\alpha = \cos^2 2\alpha - \sin 6\alpha \sin 2\alpha$
53	$2 \sin 3\alpha \sin 8\alpha = \cos 5\alpha - \cos 11\alpha$
54	$\cos^4 \alpha - \sin^4 \alpha = \cos 2\alpha$
55	$2 \cos 2\alpha = (1 - \cos 2\alpha)(\operatorname{ctg}^2 \alpha - 1)$
56	$2 \sin 2\alpha \cos \alpha - \sin 3\alpha = \sin \alpha$
57	$\frac{\sin 3\alpha - \sin \alpha}{\cos \alpha - \cos 3\alpha} = \operatorname{ctg} 2\alpha$
58	$2 \sin^2 \frac{\alpha}{2} \operatorname{tg} \alpha = \operatorname{tg} \alpha - \sin \alpha$
59	$2 \cos^2 \frac{\alpha}{2} - \cos \alpha = 1$
60	$2 \cos \alpha = (1 - \cos \alpha) \left( \operatorname{ctg}^2 \frac{\alpha}{2} - 1 \right)$

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di riepilogo

61	$\frac{1}{\csc \alpha} + \frac{1 - \sin \alpha \cos \alpha}{\cos \alpha} = \frac{\tan \alpha}{\sin \alpha}$
62	$\sin \alpha \cos \alpha \csc \alpha + \sec \alpha = \frac{2 - \sin^2 \alpha}{\cos \alpha}$
63	$\tan \alpha + \sin^2 \alpha = \frac{\sec \alpha (1 - \cos^2 \alpha)}{\sin \alpha} + \frac{\cos^2 \alpha - \cos^4 \alpha}{1 - \sin^2 \alpha}$
64	$\frac{1}{\cot \alpha} - \frac{1}{\tan \alpha} = \frac{2 \sin^2 \alpha - 1}{\sin \alpha \cos \alpha}$
65	$\sin \alpha = \frac{\tan \alpha}{\pm \sqrt{1 + \tan^2 \alpha}}$
66	$\cos \alpha = \pm \frac{\sqrt{\csc^2 \alpha - 1}}{\csc \alpha}$
67	$\frac{2 \sin^2(\pi - \alpha) - 1}{\sin \alpha \cos(2\pi - \alpha)} + \cos(-\alpha) \csc(\pi - \alpha) = \frac{1}{\cot(\pi + \alpha)}$
68	$1 + 2 \sin(2\pi - \alpha) \cos(\pi + \alpha) = [\sin(\pi - \alpha) - \cos(\pi + \alpha)]^2$
69	$\frac{1 + \cos(\pi + \alpha)}{\sin(2\pi - \alpha) \cos \alpha} = \sin \alpha - \tan \alpha - \frac{\cos(\pi + \alpha) + 1}{\tan(\pi + \alpha)}$
70	$[\sin(\pi - \alpha) - \cos(\pi - \alpha)]^2 = \frac{2 \sin(\pi - \alpha)}{\sec(2\pi - \alpha)} + 1$
71	$\frac{\tan(\pi + \alpha)}{1 - \tan^2(\pi - \alpha)} = \frac{\cot(\pi + \alpha)}{\cot^2(2\pi - \alpha) - 1}$
72	$-\sin^3(2\pi - \alpha) = \tan(\pi - \alpha)[\cos(-\alpha) + \cos^3(\pi - \alpha)]$
73	$\frac{\sin \alpha (1 + \sin \alpha) \tan(2\pi - \alpha)}{\tan \alpha} = \sin(\pi + \alpha) [1 - \sin(2\pi - \alpha)]$
74	$\frac{1}{2} \sin 2(\alpha + \beta) = \sin(\alpha + \beta) \cos(\alpha + \beta)$
75	$2 \sin(\alpha - \beta) \cos(\alpha + \beta) = \sin 2\alpha - \sin 2\beta$
76	$\cos^4 \frac{\alpha}{2} - \sin^4 \frac{\alpha}{2} = \cos \alpha$
77	$\csc \alpha + \cot \alpha = \cot \frac{\alpha}{2}$
78	$\frac{2 \sin \alpha - \sin 2\alpha}{2 \sin \alpha + \sin 2\alpha} = \tan^2 \frac{\alpha}{2}$
79	$\frac{\sin 6\alpha + \sin 2\alpha + \cos 2\alpha}{\cos 6\alpha + 2 \cos 2\alpha} = \frac{2 \tan 4\alpha + \sec 4\alpha}{2 + \sec 4\alpha}$
80	$\frac{\sin(3\alpha + \beta) \sin(3\alpha - \beta) - \sin(\alpha + \beta) \sin(\alpha - \beta)}{\sin 4\alpha \sin 2\alpha} = 1$